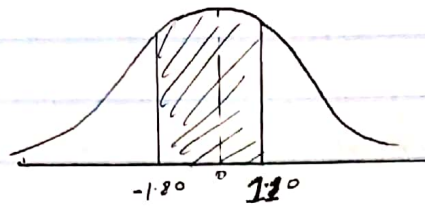


Question 1.

(a) Between $Z = 1.10$ and $Z = -1.80$

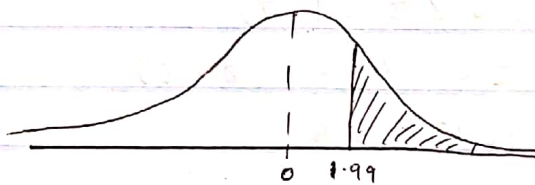


$$= P(-1.80 < Z < 1.10)$$

$$= 0.8643 - 0.0359$$

$$= 0.8284$$

(b) To the right of $Z = 1.99$

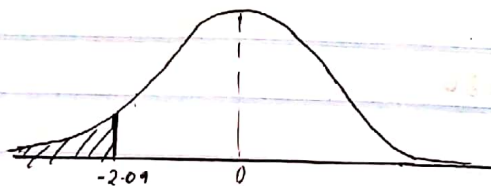


$$P(Z > 1.99) = 1 - P(Z < 1.99)$$

$$= 1 - 0.9767$$

$$= 0.0233$$

(c) To the left of $Z = -2.09$



$$= P(Z < -2.09) = 0.0183$$

Question 2

$$\bar{x} = 476$$

$$s = 22$$

(a) Between 476 and 500 passengers

$$Z(500) = \frac{500 - 476}{22} = 1.09$$

$$Z(476) = \frac{476 - 476}{22} = 0.00$$

$$\begin{aligned} P(476 < n < 500) &= P(0 < Z < 1.09) \\ &= P(Z < 1.09) - P(Z < 0) \\ &= 0.8621 - 0.5 \\ &= 0.3621 \end{aligned}$$

(b) Fewer than 450 passengers

$$Z(450) = \frac{450 - 476}{22} = -1.18$$

$$P(Z < -1.18) = 0.1190$$

(c) More than 510 passengers

$$Z(510) = \frac{510 - 476}{22} = 1.55$$

$$\begin{aligned} P(Z > 1.55) &= 1 - P(Z < 1.55) \\ &= 1 - 0.9394 \\ &= 0.0606 \end{aligned}$$

Question 3

$$\sum x = 13000$$

$$n = 27$$

$$\bar{x} = \frac{13000}{27} = 481.481$$

$$s = \sqrt{\frac{724040.7407}{27}} = 163.757$$

$$\text{Median} = 460$$

$$sk = 3 \left(\frac{481.481 - 460}{163.757} \right) = 0.3935$$

False. A skewness of 0.3935 indicates that the distribution is moderately skewed.

Question 4

$$\bar{x} = 36$$

$$n = 35$$

$$s = 3.6$$

Probability that the mean of the sample is between 34 and 37.5

$$Z(34) = \frac{34 - 36}{3.6 \div \sqrt{35}} = -3.29$$

$$Z(37.5) = \frac{37.5 - 36}{3.6 \div \sqrt{35}} = 2.47$$

$$\begin{aligned} &= P(-3.29 < z < 2.47) \\ &= P(z < 2.47) - P(z < -3.29) \\ &= 0.9932 - 0.0005 \\ &= 0.9927 \end{aligned}$$

Question 5

$$p = 0.22$$

$$n = 200$$

$$q = 1 - 0.22 = 0.78$$

$$X = 30$$

$$\mu = np = 200 \times 0.22 = 44$$

$$\sigma = \sqrt{npq} = \sqrt{200 \times 0.22 \times 0.78} = 5.858$$

$$= P(X > 30) = P(X > 30.5)$$

$$Z(30.5) = \frac{30.5 - 44}{5.858} = -2.30$$

$$\begin{aligned} P(Z > -2.30) &= 1 - P(Z < -2.30) \\ &= 1 - 0.0007 \\ &= 0.9993 \end{aligned}$$

Question 6

(a) 75%

$$(1 - 0.75) / 2 = 0.125$$

Area btw 0 and Z-score: 0.125

$$Z\text{-score} = 1.150$$

(b) 80%

$$(1 - 0.80) / 2 = 0.1$$

Area btw 0 and Z-score = 0.1

$$Z\text{-score} = 1.282$$

(c) 85%

Area between 0 and Z-score: $(1 - 0.85) / 2 = 0.075$

$$Z\text{-score} = 1.440$$

(d) 95%

$$(1 - 0.95) / 2 = 0.025$$

$$Z\text{-score} = 1.96$$

(e) 99%

Area between 0 and Z-score = 0.005

$$Z\text{-score} = 2.58$$

Question 7

$$\begin{aligned} \text{MOE} &= \frac{14.89 - 12.67}{2} \\ &= 1.11 \end{aligned}$$

Question 8

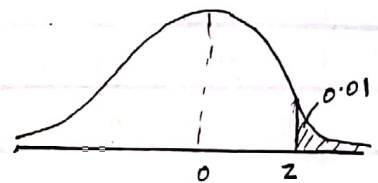
(a) $\alpha = 0.01$, right tailed test

Area between 0 and Z-score $\Rightarrow 0.5 - 0.01$

$$= 0.49$$

$$P = 0.5 + 0.49 = 0.99$$

$$Z\text{-score} = 2.63$$

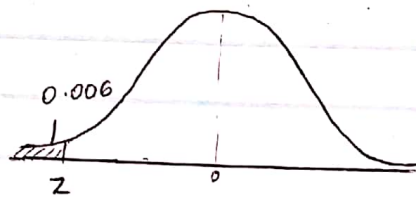


(b) $\alpha = 0.006$, left tailed test

Area between 0 and Z-score $\Rightarrow 0.5 - 0.006 = 0.494$

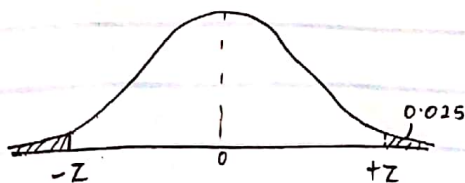
$$P = 0.006 \quad ; \quad 0.5 - 0.494$$

$$= -2.51$$



(c) $\alpha = 0.05$, two tailed test

Lower Z & upper Z



$$\frac{0.05}{2} = 0.025$$

$$p = 0.025 \text{ and } (1 - 0.025)$$

$$Z\text{-score} = -1.96 \text{ and } 1.96$$

Question 9

$$H_0: \mu = 338$$

$$H_a: \mu > 338$$

$$\alpha = 0.05$$

$$Z_c = \pm 1.64$$

Rejection region: $|Z| > 1.64$

$$Z = \frac{350 - 338}{43.2 \div \sqrt{50}} = 1.964$$

$Z = 1.964 > Z_c = 1.64$. The null hypothesis is rejected

It can be concluded that there is significant evidence to conclude that the mean number of friends is greater than 338

Question 10

$$H_0: \mu = 2.27$$

$$H_a: \mu \neq 2.27$$

$$\alpha = 0.05$$

$$t_c = \pm 2.093$$

Rejection region: $|t| > 2.093$

$$t = \frac{2.98 - 2.27}{0.98 \sqrt{20}} = 3.24$$

$t = 3.24 > t_c = 2.093$. The null hypothesis is rejected

It can be concluded that the average differs from the population average.