

LAB Solution

Step i) Calculation of horizontal distance of each point from instrument.

$$\text{Horizontal distance} = \text{Slope distance} \times \sin(\angle A)$$

From Instrument Station. To :

Point 1 : Slope = 18.548 ft.
Vertical angle $89^{\circ} 16' 18''$
Horizontal distance = 18.547 ft

Point 2 : Slope = 41.276
 $\angle = 89^{\circ} 29' 34''$
Distance = 41.274 ft

Point 3 :
Slope = 57.220 ft
 $\angle = 89^{\circ} 28' 2''$
Distance = 57.218

Point 4
Slope = 112.550 ft
 $\angle = 89^{\circ} 32' 32''$
Distance = 112.547 ft

Point 5
Slope = 46.768
 $\angle = 89^{\circ} 49' 32''$
Dist = 46.768 ft

Step ii) Calculation of latitude & departure of each point from instrument station.

$$\text{Latitude of line} = \text{Distance} \times \cos \theta$$

$$\text{Departure of line} = \text{Distance} \times \sin \theta$$

where θ is azimuth of line (Horizontal angle)

This can be tabulated in the table below.

From Instrument Station To :	Horizontal Distance (ft)	Azimuth θ	Latitude (L)	Departure (D)
Point 1	18.547	$166^{\circ} 22' 50''$	-18.025	4.367
Point 2	41.274	$112^{\circ} 23' 43''$	-15.725	38.161
Point 3	51.218	$60^{\circ} 3' 58''$	28.552	49.585
Point 4	112.547	$84^{\circ} 7' 19''$	102.719	45.996
Point 5	46.768	$33^{\circ} 54' 17''$	46.504	-4.966

Step iii) Calculation of Azimuth of each line & corresponding length of each line

$$\text{Azimuth of a line between 2 points} = \tan^{-1} \left(\frac{\text{Difference in East Coordinates}}{\text{Difference in North Coordinates}} \right)$$

$$\text{Length of line between 2 points} = \sqrt{(\text{Diff in East Coordinates})^2 + (\text{Diff in North Coordinates})^2}$$

Line 1-2

Difference in North Co = 2.300

" " East Coords 33.794

$\tan \theta = 14.69304$

Azimuth $\theta = 86^{\circ} 6' 23''$

Quadrant correction = 0°

Final azimuth $\theta = 86^{\circ} 6' 23''$

Length: 33.872 ft.

Line 2-3

$$\text{Diff in N. Coord} = 44.277$$

$$\text{" " E. Coord} = 17.424$$

$$\text{Tan } \theta = 0.25801$$

$$\text{Azimuth } \theta = 14^{\circ} 28' 23''$$

$$\text{Quadrant Correction} = 0^{\circ}$$

$$\text{Final Azimuth } \theta = 14^{\circ} 28' 3''$$

$$\text{Length} = 45.727 \text{ ft.}$$

Line 3-4

$$\text{Diff in N. Coord} = 74.167$$

$$\text{" " E. Coord} = -3.582$$

$$\text{Tan } \theta = -0.04839$$

$$\text{Azimuth } \theta = -2^{\circ} 46' 14''$$

$$\text{Quadrant Correction} = 360^{\circ}$$

$$\text{Final Azimuth } \theta = 357^{\circ} 13' 46''$$

$$\text{Length} = 74.254 \text{ ft.}$$

Line 4-5

$$\text{Diff in N. Coord} = -56.215$$

$$\text{" " E. Coord} = -50.962$$

$$\text{Tan } \theta = 0.90656$$

$$\text{Azimuth } \theta = 42^{\circ} 11' 39''$$

$$\text{Quadrant Correction} = 180^{\circ}$$

$$\text{Final Azimuth } \theta = 222^{\circ} 11' 39''$$

$$\text{Length} = 75.877 \text{ ft.}$$

Line 5-1

$$\text{Diff in N. Coord} = -64.529$$

$$\text{Diff in E. Coord} = 9.333$$

$$\tan \theta = -0.14463$$

$$\text{Azimuth } \theta = -8^{\circ} 13' 47''$$

$$\text{Quadrant Correction} = 180^{\circ}$$

$$\text{Final Azimuth } \theta = 171^{\circ} 46' 13''$$

$$\text{Length} = 65.2 \text{ ft}$$

Step 84) Interior Angles Between Lines

To get this we have to calculate the counter-clockwise traverse.

$$\therefore \text{Angle between lines} = \text{azimuth of preceding line} - \text{azimuth of back line} + 180$$

$$\angle \text{Point 1} = 86^{\circ} 6' 23'' - (171^{\circ} 46' 13'' + 180^{\circ}) = 94^{\circ} 20' 10''$$

$$\angle \text{Point 2} = 14^{\circ} 28' 3'' - (86^{\circ} 6' 23'' + 180^{\circ}) = 108^{\circ} 21' 40''$$

$$\angle \text{Point 3} = 351^{\circ} 13' 46'' - 14^{\circ} 28' 3'' + 180^{\circ} = 162^{\circ} 45' 43''$$

$$\angle \text{Point 4} = 222^{\circ} 11' 39'' - 351^{\circ} 13' 46'' + 180^{\circ} = 44^{\circ} 57' 53''$$

$$\angle \text{Point 5} = 171^{\circ} 46' 13'' - 222^{\circ} 11' 39'' + 180^{\circ} = 129^{\circ} 34' 34''$$