

SECTION A

$$1. IQR = Q_3 - Q_1$$

Data	1	3	4	5	5	6	7	11
Rank	1	2	3	4.5	4.5	6	7	8

$$k = \frac{3}{4}(n+1) = \frac{3}{4}(8+1) = 6.75$$

$$Q_3 = 6 + (6.75 - 6)(7 - 6)$$

$$= 6 + 0.75 = 6.75$$

$$k \text{ for } Q_1 = \frac{1}{4}(n+1) = \frac{1}{4}(9) = 2.25$$

$$Q_1 = 2 + (2.25 - 2)(4 - 3)$$

$$= 2 + (0.25)(1) = 2.25$$

$$IQR = Q_3 - Q_1 = 6.75 - 2.25 = 4.5 = 4.5$$

$$2. \text{ Inverse of } f(x) = \frac{9x+5}{6}$$

$$\text{let } f(x) = y$$

$$y = \frac{9x+5}{6}$$

Interchanging variables

$$x = \frac{9y+5}{6}$$

$$6x = 9y + 5$$

$$6x - 5 = 9y$$

$$y = \frac{6x-5}{9}$$

$$\therefore f^{-1}(x) = \frac{6x-5}{9}$$

$$3. \text{ Red} = 3$$

$$\text{Blue} = 2$$

$$\text{Green} = 5$$

$$P(\text{red}') = 1 - P(\text{red})$$

$$= 1 - \frac{3}{10} = \frac{7}{10}$$

4. There are 26 options for ~~any~~ ^{first} letter of the password
therefore

$$\text{No. of passwords} = 26 \times 25 \times 24 \times 23 = 358800$$

2nd letter has 25 options

3rd letter has 24 options

4th letter has 23 options.

5. $(1, -3)$

$$m_1 = 4$$

$$m_1 m_2 = -1$$

$$4 m_2 = -1$$

$$m_2 = -\frac{1}{4}$$

Let the other unknown points = (x, y)

$$(x, y) (1, -3) \quad m = -\frac{1}{4}$$

$$G = \frac{\Delta y}{\Delta x} = \frac{y+3}{x-1} = -\frac{1}{4}$$

$$4y+12 = -x+1$$

$$4y = -x-11$$

$$y = -\frac{x}{4} - \frac{11}{4}$$

6. (2) The tip of the U shape is the minimum point

(i) Min point = $(-2, 1)$

(ii) $y = x^2 + 4x + 5$

Between -5 and -2 the function is decreasing

Between -2 and 1 the function is increasing

7. (i) $\frac{d}{dx}(6x^2)$

Using nth rule

$$\frac{d}{dx}(6x^2) = 12x$$

$$\text{vi) } \frac{d}{dx} \cos 5x = -5 \sin 5x$$

$$\text{vii) } x^{-2}$$

$$\frac{d}{dx} (x^{-2}) = -2x^{-3} = \frac{-2}{x^3}$$

$$\text{8. } \text{v) } \int 5x^3 dx = \frac{5x^{3+1}}{3+1} + C = \frac{5}{4}x^4 + C$$

$$\text{vi) } \int 4x dx = \frac{4x^2}{2} = 2x^2$$

$$\text{vii) } \int e^x dx = \frac{1}{1} e^{fx} = 1e^x = e^x$$

$$\text{9. } (11 - 6i) - (4 - 3i) = (11 - 4) + (-6 - (-3))i \\ = 7 - 3i$$

$$\text{10. } (4 - 12i)(3 - 8i)$$

Using the foil formula.

$$\begin{aligned} (4 - 12i)(3 - 8i) &= 12 - 32i - 36i + 96i^2 \\ &= 12 - 68i - 96 \\ &= 12 - 96 - 68i \\ &= -84 - 68i \end{aligned}$$

SECTION B

1. Modelling using mathematics

$$\text{Speed} = \frac{\text{Distance}}{\text{time}} \Rightarrow S = \frac{D}{t}$$

Rearranging $D = S \times t = S * t$

If speed $S = 320 \text{ km/h}$

$$t = 15 \text{ mins} = \frac{15}{60} = \frac{1}{4} \text{ hrs.}$$

$$D = S \times t = 320 \times \frac{1}{4} = 80 \text{ km}$$

b) $S = ut + \frac{1}{2} at^2$ where $u = \text{initial speed}$, t is time,
 a is acceleration

$$v^2 = u^2 + 2as$$

on dry concrete $a = -7.00 \text{ m/s}^2$

wet concrete $a = -5.00 \text{ m/s}^2$

from physics $v^2 = u^2 + 2as$ $v = 0$ being final speed.

$$v^2 = u^2 + 2as \quad \text{on dry concrete}$$

$$0 = 30^2 - 2(7)s$$

$$\frac{30^2}{14} = s = 64.29 \text{ m}$$

On wet concrete

$$v^2 = u^2 + 2as$$

$$0 = 30^2 + 2(-5)s$$

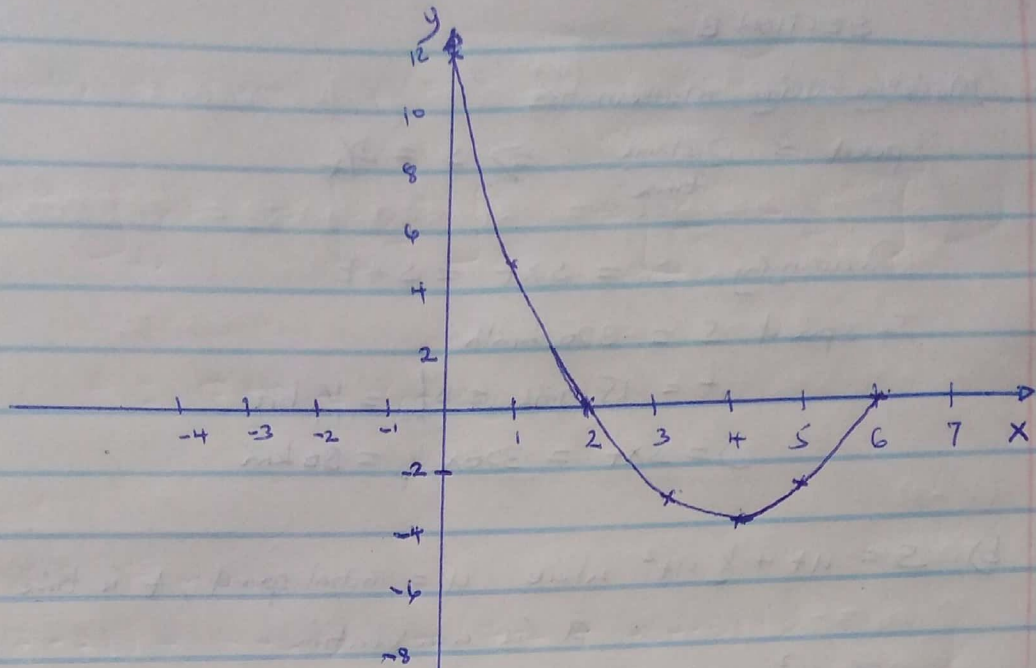
$$\frac{30^2}{10} = \frac{10}{10} s \Rightarrow s = 90 \text{ m}$$

2. Statistics and probability

3. Functions and Graphs

$$y = x^2 - 8x + 12. \quad \text{for } 0 \leq x \leq 6$$

X	0	1	2	3	4	5	6
Y	12	5	0	-3	-4	-3	0



(i) X-intercepts $(2, 0)$ and $(6, 0)$

(ii) Range for the domain $0 \leq x \leq 6$ is $0-12$ or $12-0$

(iii) Turning point = $(4, -4)$ Lowest point from the graph

SECTION C

1. Calculus

$$(i) \frac{dy}{dx} (3x^2+1)^5$$

$$y = (3x^2+1)^5 \quad \text{Chain rule is used in this case}$$

$$\text{Let } u = 3x^2+1 \quad \frac{du}{dx} = 6x$$

$$\text{Therefore } y = u^5 \quad \frac{dy}{du} = 5u^4$$

$$\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$$

$$\frac{dy}{dx} = 5u^4 \cdot 6x \quad \text{but } u = (3x^2+1)$$

$$\therefore \frac{dy}{dx} = 5(3x^2+1)^4 \cdot 6x$$

$$(ii) y = \frac{5x^2-3x}{2x^4} \quad \text{using Quotient rule}$$

$$\frac{dy}{dx} = \frac{u'v - v'u}{v^2} \quad \text{where } 5x^2-3x = u \quad \frac{du}{dx} = 10x-3$$

$$2x^4 = v \quad \frac{dv}{dx} = 8x^3$$

$$\frac{dy}{dx} = \frac{(10x-3)(2x^4) - 8x^3(5x^2-3x)}{(2x^4)^2}$$

$$\frac{dy}{dx} = \frac{20x^5 - 6x^4 - 40x^5 + 24x^4}{4x^8}$$

$$\frac{dy}{dx} = \frac{20x^5}{4x^8} - \frac{6x^4}{4x^8} - \frac{40x^5}{4x^8} + \frac{24x^4}{4x^8}$$

$$= 5x^{-3} - \frac{6}{4x^4} - \frac{10}{x^3} + \frac{6}{x^4}$$

$$= \frac{5}{x^3} - \frac{6}{4x^4} - \frac{10}{x^3} + \frac{6}{x^4}$$

$$(b) s(t) = t^3 - 12t^2 + 45t$$

$$(i) \frac{ds(t)}{dt} = v = 3t^2 - 24t + 45$$

$$\text{When } t = 2.$$

$$v = 3(2^2) - 24(2) + 45 = 9 \text{ m/s}$$

$$a = \frac{dv}{dt} = 6t - 24$$

$$\text{When } t = 2 \quad a = 6(2) - 24 = -12 \text{ m/s}^2$$

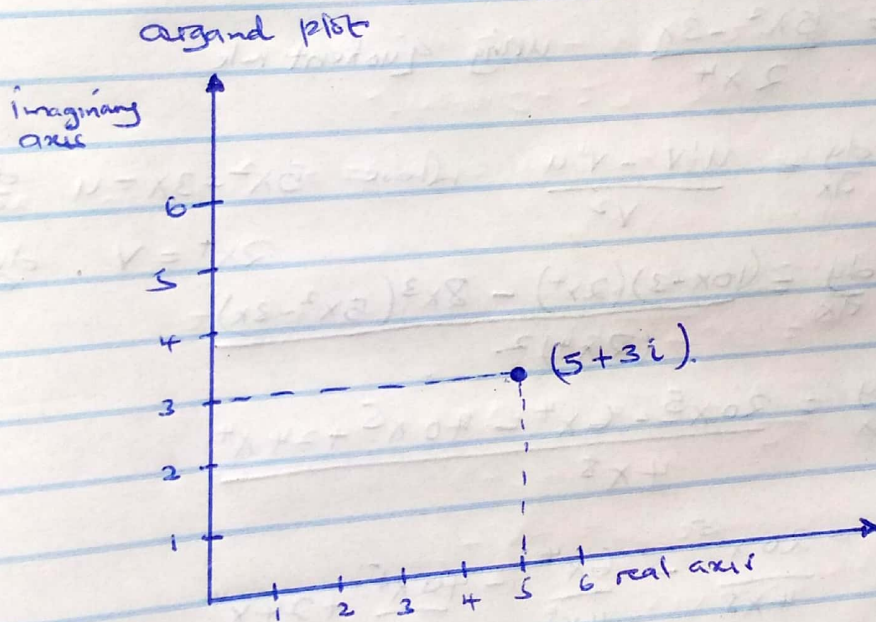
1) Area under the curve $f(x) = x^3$ between $x=2$ and $x=4$

$$A = \int_2^4 x^3 = \left[\frac{x^4}{4} \right]_2^4 = \left[\frac{4^4}{4} - \frac{2^4}{4} \right]$$

$$A = \frac{240}{4} = 60 \text{ sq. units}$$

2. Complex numbers

$$\begin{aligned} \text{a) } (7-2i) - (2-5i) &= (7-2 + (2-5)i) \\ &= 5 + 3i \end{aligned}$$



$$\text{b) } \frac{6-4i}{5+4i} \quad a=6, b=-4, c=5, d=4$$

$$\begin{aligned} \text{We know that } \frac{a+bi}{c+di} &= \frac{ac+bd + (bc-ad)i}{c^2+d^2} \\ &= \frac{6(5) + (-4)(4) + ((-4)(4) - 6(4))i}{5^2+4^2} \\ &= \frac{30-16 + -40i}{41} \\ &= \frac{14-40i}{41} = \frac{14}{41} - \frac{40}{41}i \end{aligned}$$

$$d) x^2 - 2x + 10 = 0 \quad a = 1, b = -2, c = 10$$

Using quadratic formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{2 \pm \sqrt{4 + (4 \times 10)}}{2} = \frac{2 \pm 6.633}{2}$$

$$x = 4.3166 \text{ or } x = -2.3165$$