

Consider the system of ODEs

$$x' = y$$

$$y' = -x + x^3.$$

- a) Find all the critical points.
- b) Find the corresponding linear system near each critical point.
- c) Classify their types using Theorem 9.3.3.