

ICS Problem Sheet #10

Problem 10.1: *fold function duality*

(2+2+2 = 6 points)

The fold functions compute a value from a list by applying an operator to the list elements and by using a neutral element. The foldl function assumes that the operator is left associative, the foldr function assumes that the operator is right associative. For example, the function call

```
foldl (+) 0 [3,5,2,1]
```

results in the computation of $((((0+3)+5)+2)+1)$ and the function call

```
foldr (+) 0 [3,5,2,1]
```

results in the computation of $(3+(5+(2+(1+0))))$. The value computed by the fold functions may be more complex than a simple scalar. It is very well possible to construct a new list as part of the fold. For example:

```
map' :: (a -> b) -> [a] -> [b]
map' f xs = foldr (\x acc -> f x : acc) [] xs
```

The evaluation of `map' (+3) [1,2,3]` results in the list `[4,5,6]`. There are several duality theorems that can be stated for the fold functions. Proof the following three duality theorems:

- a) Let `op` be an associative operation with `e` as the neutral element. Then the following holds for finite lists `xs`:

$$\text{foldr } op \ e \ xs = \text{foldl } op \ e \ xs$$

- b) Let `op1` and `op2` be two operations for which

$$\begin{aligned} x \text{ 'op1'} (y \text{ 'op2'} z) &= (x \text{ 'op1'} y) \text{ 'op2'} z \\ x \text{ 'op1'} e &= e \text{ 'op2'} x \end{aligned}$$

holds. Then the following holds for finite lists `xs`:

$$\text{foldr } op1 \ e \ xs = \text{foldl } op2 \ e \ xs$$

- c) Let `op` be an associative operation and `xs` a finite list. Then

$$\text{foldr } op \ a \ xs = \text{foldl } op' \ a \ (\text{reverse } xs)$$

holds with

$$x \text{ op'} y = y \text{ op } x$$

Problem 10.2: fork system call

(1+3 = 4 points)

Consider the following C program (let me call the source file `happy-fork.c`.)

```
#include <unistd.h>

int main(int argc, char *argv[])
{
    for (; argc > 1; argc--) {
        if (0 == fork()) {
            (void) fork();
        }
    }
    return 0;
}
```

a) Assume the program has been compiled into `happy-fork` and that all system calls succeed at runtime. How many child processes are created for the following invocations of the program:

- `./happy-fork`
- `./happy-fork a`
- `./happy-fork a b`
- `./happy-fork a b c`
- `./happy-fork a b c d`

b) Write a Linux assembly program (x86 64-bit Linux) using the GNU assembler that does the same as the C program shown above. It should in addition print `x\n` right before exiting. The assembly code should invoke the system calls directly, do not use any library calls. See `hello-asm-syscall.s` in the lecture notes as a starting point. Compile your assembly code with `gcc -nostdlib -static`. Make sure your assembly code has proper comments so that we can understand it.

The `fork()` system call number is 57 on Linux. You can find the value of `argc` at `(%rsp)` at `_start`.